Modelling of compressive strength of self-compacting concrete containing fly ash by gene expression programming

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Abstract
In the modelling study, two models are presented by gene expression programming (GEP) for estimation of compressive strength ($f_c$) of self-compacting concrete (SCC) produced with fly ash (FA). The main difference between two models is the number of heads determined in the development of models. Two established models are proposed to predict the $f_c$ values by utilizing the amount of cement, water, FA, coarse and fine aggregate, superplasticiser and age of specimen as input values for SCC mixtures. In the establishment of proposed models, 516 $f_c$ values are utilized. These values were obtained from 34 different published scientific experimental studies on the SCC produced with FA. The training and testing sets employed in the creation of models consist of 368 $f_c$ results of SCC mixtures. The models are validated with the remaining 148 $f_c$ results of SCC mixtures, which are not employed in training and testing sets. The estimated $f_c$ results attained from established models were compared with $f_c$ results of experimental studies, and previously proposed artificial neural network (ANN) model. These comparisons and the results of statistical evaluation have strongly revealed that the results of established models match well with the experimental results, and they are considered very reliable.

Keywords: Self-compacting concrete, Fly ash, Compressive strength, Gene expression programming.

Introduction
Self-compacting concrete (SCC) is a type of concrete evolved in Japan in the 1980s, and later this type of concrete is adopted in the rest of the world. The main property of fresh SCC is capable of spreading under its own weight without vibration. Therefore, it can self-settle without any blocking and segregation (Ozawa, Maekawa, & Okamura, 1990; Siddique, Aggarwal, & Aggarwal, 2012b; Sonebi, 2004). Moreover, this type of fresh concrete has three important characteristics which are passing capacity, segregation resistance and filling capacity (Golafshani, Rahai, & Sebt, 2014; Liu, 2010; Melo & Carneiro, 2010; Siddique, 2011; Sonebi, 2004; Zhu, Gibbs, & Bartos, 2001). The mixtures of SCC are different in comparison to traditional concrete. The SCC incorporates such chemical admixtures that provide high flowability. Further more, the water to binder ratio and the ingredient of coarse aggregate of SCC are lower than those of traditional concrete to improve the workability and decrease segregation (Bingöl & Tohumcu, 2013; Golafshani & Pazouki, 2018; Khatib, 2008; Mohamed, 2011; Sonebi, 2004). Currently, the SCC has gained wide usage area for structural configurations and different structural applications. Chemical additives used as superplasticizer can increase the cost of SCC (Bouzoubaa & Lachemi, 2001). However, the un-use of a vibrator in the placement of SCC reduces cost and provides balance. On the other hand, the employment of mineral admixtures like fly ash (FA) and ground blast furnace slag improves the workability of SCC without raising its cost, where asthey result with a decrease in the amount of superplasticiser used in the mixtures (Bingöl & Tohumcu, 2013; Siddique, 2011).

FA is a fine-grained residual material obtained from coal combustion in thermal power plant. In general, FA is used by partial replacement with cement in the traditional concrete and in the SCC as a mineral admixture. The employment of FA in concrete mixture improves workability, impermeability and in later years mechanical properties of concrete (Bouzoubaa & Lachemi, 2003; Le & Ludwig, 2016; Sonebi, 2004; Sukumar, Nagamani, & Srinivasa Raghavan, 2008). The partial substitution of FA with Portland cement significantly advances rheological properties of concrete; therefore, the concrete made with FA requires less superplasticizer to gain a similar workability crosschecked to concrete made with only Portland cement (Khatib, 2008; Le & Ludwig, 2016; Siddique, 2011; Yahia, Tanimura, Shimabukuro, & Shimoyama, 1999).

The compressive strength ($f_c$) of concrete is one of the most considerable parameter in the design of concrete and reinforced concrete structures. The $f_c$ value of concrete is determined by experiments, and the $f_c$ is closely related with concrete constituents and their ratios. Recently, the soft computing methods with the inclusion of genetic programming, genetic algorithm, neural networks and fuzzy logic have been usually utilized to resolve many complex problems in the engineering areas. Moreover, the prediction algorithms like neural network (Eskandari-Naddaf & Kazemi, 2017; Nagarajan, Rajagopal, & Meyappan, 2020; Nakata, Fernández, Carrillo, Haro, & Pinaud, 2018), fuzzy logic (Topçu & Sandemir, 2008), genetic algorithm (Acar Yildirim & Akcay, 2019; Lim, Yoon, & Kim, 2004; Prendes-Gero, Bello-Garcia,
Coz-Díaz, Suárez-Domínguez, & Nieto, 2018), gene expression programming (GEP) (Mahdinia, Eskandari-Naddaf, & Shadnia, 2019) are the most commonly employed methods in the concrete research area to estimate the demanded properties of concrete in design of concrete mixtures to save time and cost.

GEP is a method like genetic programming and genetic algorithms. Main difference between three algorithms exists in the character of individuals. The individuals are nonlinear existences of different shapes and sizes in genetic programming. The individuals are linear sequences of fixed length (chromosomes) in genetic algorithms. The individuals are encoded as linear existences of fixed length that are after wards enounced as nonlinear existences of different shapes and sizes (i.e., simple diagram exhibitions or ETs) in GEP. The coaction of chromosomes and ETs in GEP imports a clear interpretation scheme for interpreting the language of chromosomes into the language of ETs. The varied sets of genetic operators improved to present genetic variety in GEP populations every time procreates prevailing ETs. GEP is highly ambidextrous and far exceeds existing evolutionary techniques (Ferreira, 2001a). Also important is that GEP chromosomes are multigenic, encoding multiple ETs or sub-programs that can be organized into a much more complex program. GEP method has been employed to estimate many properties of concrete in civil engineering. The influence of sample size and shape on the $f_c$ of concrete with FA (Saridemir, 2014), the $f_c$ of high performance concrete (Mousavi, Aminian, Gandomi, Alavi, & Bolandi, 2012), the $f_c$ of mortar (Baykasoğlu, Dereli, & Taniş, 2004), the $f_c$ of lightweight concrete (Jafari & Mahini, 2017), the splitting tensile strength from the $f_c$ of concrete (Severcan, 2012), the mechanical properties of concrete produced with recycled aggregate (Gholampour, Gandomi, & Ozbakkaloglu, 2017), the $f_c$ of mortar (Mahdinia et al., 2019), the elasticity modulus of normal-strength concrete and high-strength concrete (Gandomi, Alavi, Ting, & Yang, 2013; Saridemir & Severcan, 2016), the split tensile strength and water permeability of high strength concrete (Nazari & Riahi, 2011), the total specific pore volume of inorganic polymers made from seeded FA and rice husk–bark ash (Nazari, 2019b), the $f_c$ of lightweight aluminosilicate geopolymers produced by fine fly ash and rice husk bark ash together with palm oil clinker aggregates (Nazari, 2019a) and the effect of SiO$_2$ and Al$_2$O$_3$ nanoparticles on the $f_c$ of ash-based geopolymers (Nazari & Riahi, 2013) were predicted by using the GEP method.

The characteristics of SCC produced with FA have been investigated by many researchers. However, with the mathematical formulas, the studies predicting the $f_c$ results of SCC produced with FA are very rare in the literature. Therefore, this modelling study has been made to predict the $f_c$ results of SCC produced with FA by using the GEP method. In this modelling study, two models are established in the GEP to estimate the $f_c$ of SCC produced with FA. The main difference between two models is the number of heads used in the development of models. These models are proposed to predict the $f_c$ values by utilizing the amount of cement, water, FA, coarse and fine aggregate, superplasticiser, and age of specimen of SCC mixtures. In the creation of the proposed models, 516 $f_c$ results obtained from the experimental studies of the SCC produced with FA at 1, 7, 14, 28, 56, 82, 90, 130, 180 and 365 days in 34 different scientific studies are used. 290 and 78 $f_c$ results of these experimental studies are employed in the training and testing sets of the established models, respectively. The remaining 148 $f_c$ results of these experimental studies that are not employed in the training and testing sets were also used to validate the models. The predicted compressive strength ($f_{c_{pred}}$) results attained from the GEP models are crosschecked with the experimental compressive strength ($f_{c_{exp}}$) results, and previously proposed ANN model (Golafshani & Pazouki, 2018). These comparisons and statistical analyses have revealed that the results of the GEP models are well matched with the experimental work results and are very reliable.

Experimental database

In order to estimate the $f_c$ values of SCC produced with FA by using the GEP models, the experimental data were collected from the literature. The experimental databases consisting of 368 experimental results collected from 25 different literature were used in the training and testing sets of models to be developed in the GEP. The experimental studies, forming the experimental databases used in the training and testing sets, were performed by utilizing results of literature (Abdalhmid, Ashour, & Sheehan, 2019; Bingöl & Tohumcu, 2013; Bouzoubaa & Lachemi, 2001; Bui, Akkaya, & Shah, 2002; Da Silva & De Brito, 2015; El-Chabib & Syed, 2013; Gesoğlu & Özbay, 2007; Güneyisi, Gesoğlu, Al-Goody, & Ipek, 2015; Güneyisi, Gesoğlu, & Özbay, 2010; Khatib, 2008; Le & Ludwig, 2016; Leung, Kim, Nadeem, Jaganathan, & Anwar, 2016; Liu, 2010; Mohamed, 2011; Patel, Hossain, Shehata, Bouzoubaa, & Lachemi, 2004; Pathak & Siddique, 2012; Pofale & Deo, 2010; Sahmaran, Lachemi, Erdem, & Yücel, 2011; Siad, Mesbah, Mouli, Escadeillas, & Khelafi, 2014; Siddique, Aggarwal, & Aggarwal, 2012a; Sonebi, 2004; Sonebi & Cevik, 2009; Sukumaran et al., 2008; Ulucan, Türk, & Karataş, 2008; Zhao, Sun, Wu, & Gao, 2015). The cement (C), water (W), FA, coarse aggregate (C-agg), fine aggregate (F-agg), superplasticizer (SP) used in the SCC mixtures besides the age of specimen (AS) were employed as input parameters in the training, testing and validation sets of models. The $f_{c_{exp}}$ values of these concrete mixtures were employed as output parameter in the training and testing sets of models. Considering the ANN model previously created by Golafshani and Pazouki (Golafshani & Pazouki, 2018) the training and testing sets were chosen from these databases without any planning where 368 experimental studies of these databases were used in the training set, while 78 experimental
studies were used in the testing set. The experimental databases consisting of 148 experimental studies collected from 9 different literature were employed in the validation set that was not employed in the training and testing sets to evaluate the performance and acceptability of developed models. The experimental studies, forming the experimental databases used in the validation set, were performed by (Ashtiani, Scott, & Dhakal, 2013; Jalal, Fathi, & Farzad, 2013; Khan & Sharma, 2015; Krishnapal, Rajeve, & Kumar, 2012; Madihalli, Saunshi, & Thakai, 2016; Satish, Kumar, & Rai, 2017; Siddique, 2011; Siddique et al., 2012b; Wang, Zhang, Wang, & Yu, 2018). The physical, chemical and mechanical properties of the materials obtained from 34 different experimental studies and used as input parameters are different as stated in these studies. Moreover, the amounts of these materials were used differently in the mixtures, and their mixtures and experimental studies were also made differently. Therefore, the $f_{c-exp}$ values used as output parameters were obtained differently. Figure 1 shows the distributions of variables employed as input parameters in response to the $f_{c-exp}$ values employed as output parameters. Besides, the descriptive statistics of inputs and output with the inclusion of maximum (Max), minimum (Min), average (Ave) and standard deviation (SD) of all sets and data count used in the sets are imparted in Table 1 for all databases.

![Figure 1. Distribution of (a) $f_{c-exp}$ and cement values, (b) $f_{c-exp}$ and water values, (c) $f_{c-exp}$ and fly ash values (d) $f_{c-exp}$ and coarse aggregate values, (e) $f_{c-exp}$ and fine aggregate values, (f) $f_{c-exp}$ and superplasticizer values and (g) $f_{c-exp}$ and age of specimens values. Source: Self-elaboration.](image)

<table>
<thead>
<tr>
<th>Data type</th>
<th>Data count</th>
<th>Statistical parameters</th>
<th>$C$ ($\text{kg/m}^3$)</th>
<th>$W$ ($\text{kg/m}^3$)</th>
<th>$\text{C}_{\text{agg}}$ ($\text{kg/m}^3$)</th>
<th>$\text{F}_{\text{agg}}$ ($\text{kg/m}^3$)</th>
<th>SP (%)</th>
<th>AS (day)</th>
<th>$f_{c-exp}$ (MPa)</th>
</tr>
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<tbody>
<tr>
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<td>516</td>
<td>Min</td>
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<td>102.00</td>
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<td>530.00</td>
<td>434.00</td>
<td>1.00</td>
<td>4.00</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Max</td>
<td>622.00</td>
<td>295.20</td>
<td>427.50</td>
<td>1426.00</td>
<td>1820.00</td>
<td>4.60</td>
<td>365.00</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Ave</td>
<td>318.08</td>
<td>188.20</td>
<td>151.15</td>
<td>822.82</td>
<td>859.27</td>
<td>1.29</td>
<td>41.74</td>
</tr>
<tr>
<td></td>
<td></td>
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<td>35.45</td>
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<td>193.62</td>
<td>186.76</td>
<td>1.07</td>
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<td>Min</td>
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<td>135.45</td>
<td>0.00</td>
<td>590.00</td>
<td>434.00</td>
<td>1.00</td>
<td>4.00</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Max</td>
<td>622.00</td>
<td>295.20</td>
<td>427.50</td>
<td>1190.00</td>
<td>1109.00</td>
<td>4.60</td>
<td>365.00</td>
</tr>
</tbody>
</table>

![Table 1. Input and output limits employed in the GEP. Source: Self-elaboration.](image)
Gene expression programming (GEP) was evolved by Ferreira (Ferreira, 2001b) using genetic algorithms and genetic programming. GEP is a soft computing method, developed in different shapes and sizes by coding constant-length linear chromosomes. In GEP technique, there are two important components. The first of these is chromosomes. The other is expression trees (ETs). The genetic information code constitutes a free mutual effect between the ETs and the chromosomes (Ferreira, 2001a; Sarıdemir, 2010; Severcan, 2012). In GEP technique, chromosomes constituted in the shape of ETs can be expressed in diverse shapes and sizes by operators and processors. In general, the chromosomes are formed of more than one equal length gene. In addition, the structural and functional organization of chromosomes creates genetic operators such as replication, recombination, mutation and transposition. These genetic operators and processors derive appropriate functions by converting non-linear variables of fixed numbers and lengths into linear arrays of different shapes and sizes (Ferreira, 2001a; Kara, 2011; Sandemir, 2010).

All problems, the simplest or the most complex ones, can be expressed by ETs in the GEP. These ETs consist of operators, functions, constants and variables. The relationships between the variables can be expressed with the ET structure (Ferreira, 2001a). Gene numbers, as well as head length, are determined for each problem with respect to the complexity of the problem. The solution of complex problems requires long chromosome structures in the ETs. Because each gene is coded as a smaller and simpler form, then it allows a spatial organization to be a complex structure. Therefore, each genetic code of Sub-unit ET and Sub-ETs is used to solve the problem. Sub-ETs are combined with link functions. These link functions are addition, subtraction, multiplication and division operations.

### Development of GEP models

In the study, in order to estimate the $f_c$ values at different ages of SCC produced with FA, four steps were taken into consideration on the models developed in the GEP technique. First, the fitness function was selected to reach the aim correctly in the prediction of $f_c$ values. The most important advantage of the selected fitness functions is that the system can find the most appropriate solution for it self. Second, the terminals and functions were selected for creating the chromosomes. The terminals and functions consist of independent variables. The selection of the appropriate set of functions is not clear, but a good estimate can be made by including all the necessary functions. In this situation, four basic arithmetic operators (+, -, *, /) and some basic functions (Mul3, Add3, Exp, Inv) can be selected. Third, the head size and the number of genes to compose the ETs (the chromosomal architecture) were selected. For GEP-based formulations, first, single gene and 2 lengths of heads are used, then the number of genes and heads are increased for the most suitable solution. In the last step the linking function, connecting the Sub-ETs, was selected. In GEP based formulations, multiplication, addition, subtraction and division can be used as linking function. According to these selected steps, two models were developed in the GEP technique to estimate $f_c$ values of SCC produced with FA at different ages. In the training and testing of these developed models, $C$, $W$, $FA$, $C_{agg}$, $F_{agg}$, $SP$ and $AS$ values were used as input (terminals), and $f_{c-exp.}$ values were used as output. Here, 290 and 78 of the experimental results were used for training and testing, respectively. The training and testing sets were determined by taking into account the ANN model previously developed by Golafshani and Pazouki (Golafshani & Pazouki, 2018). In their proposed ANN model, 270 of the experimental results were employed for training, and 68 of the experimental results were employed for testing. However, in the ANN model previously developed, $d_2 = FA$ input variable did not have a value of 0, and in order to develop more comprehensive models, new literature data were added to the training and testing sets of GEP models. The definitions function set and the details of other steps used in both GEP models developed with considering the Sub-ETs (gene number or Sub-ETs) and head size on the third step were presented in Table 2. Besides, the effect of genes number on the performance of the models was determined by keeping the chromosome number and head size constant.

<table>
<thead>
<tr>
<th></th>
<th>Ave</th>
<th>192.34</th>
<th>168.18</th>
<th>812.83</th>
<th>816.37</th>
<th>1.08</th>
<th>41.48</th>
<th>35.93</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>SD</td>
<td>106.10</td>
<td>293.33</td>
<td>79.48</td>
<td>123.45</td>
<td>121.78</td>
<td>1.08</td>
<td>61.91</td>
</tr>
<tr>
<td>Testing</td>
<td>Min</td>
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<td>135.45</td>
<td>0.00</td>
<td>590.00</td>
<td>478.00</td>
<td>0.00</td>
<td>1.00</td>
</tr>
<tr>
<td></td>
<td>Max</td>
<td>622.00</td>
<td>295.20</td>
<td>373.00</td>
<td>1058.20</td>
<td>1109.00</td>
<td>4.60</td>
<td>365.00</td>
</tr>
<tr>
<td></td>
<td>Ave</td>
<td>307.81</td>
<td>191.56</td>
<td>169.18</td>
<td>819.61</td>
<td>822.13</td>
<td>0.93</td>
<td>37.32</td>
</tr>
<tr>
<td></td>
<td>SD</td>
<td>111.78</td>
<td>32.55</td>
<td>76.17</td>
<td>107.20</td>
<td>109.27</td>
<td>0.94</td>
<td>53.40</td>
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<tr>
<td>Validation</td>
<td>Min</td>
<td>86.00</td>
<td>102.00</td>
<td>0.00</td>
<td>530.00</td>
<td>605.00</td>
<td>0.20</td>
<td>3.00</td>
</tr>
<tr>
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<td>Max</td>
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<td>246.00</td>
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<td>1820.00</td>
<td>4.20</td>
<td>365.00</td>
</tr>
<tr>
<td></td>
<td>Ave</td>
<td>339.08</td>
<td>178.31</td>
<td>108.26</td>
<td>844.10</td>
<td>962.89</td>
<td>1.89</td>
<td>44.59</td>
</tr>
<tr>
<td></td>
<td>SD</td>
<td>124.21</td>
<td>44.72</td>
<td>56.05</td>
<td>306.82</td>
<td>266.81</td>
<td>0.85</td>
<td>81.35</td>
</tr>
</tbody>
</table>

SD is standard deviation, C is Cement, W is Water, FA is Fly Ash, $C_{agg}$ is Coarse Aggregate, $F_{agg}$ is Fine Aggregate, SP is Superplasticizer, and AS is Age of Specimen.
in the models. The values in the other definitions are the numbers determined by the GEP technique which shows the effectiveness of the GEP operators mentioned above.

### Table 2. Variables employed in the GEP. Source: Self-elaboration.

<table>
<thead>
<tr>
<th>Descriptions</th>
<th>GEP-I</th>
<th>GEP-II</th>
</tr>
</thead>
<tbody>
<tr>
<td>Function set</td>
<td>+, -, *, /, Add3, Mul3, Csc, Tan, Sin, Ln, X2, Inv</td>
<td>+, -, *, /, Sqrt, Sub3, Add3, Mul3, Inv, Pow, Tan, Exp, Cos, Ln</td>
</tr>
<tr>
<td>Number of genes</td>
<td>4</td>
<td>5</td>
</tr>
<tr>
<td>Constants per gene and head size</td>
<td>10</td>
<td>Multiplication</td>
</tr>
<tr>
<td>Linking function</td>
<td>Multiplication</td>
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</tr>
<tr>
<td>Inversion</td>
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<td></td>
</tr>
<tr>
<td>Mutation</td>
<td>0.00206</td>
<td></td>
</tr>
<tr>
<td>One or two-point recombination</td>
<td>0.00277</td>
<td></td>
</tr>
<tr>
<td>Transposition and gene recombination</td>
<td>0.00277</td>
<td></td>
</tr>
<tr>
<td>Random chromosomes</td>
<td>0.00260</td>
<td></td>
</tr>
</tbody>
</table>

Sqrt=Square root, Sub3=Subtraction with 3 inputs, Add3=Addition with 3 inputs, Mul3=Multiplication with 3 inputs, Csc=Cosecant, Inv=Inverse, Pow=Power and Exp=Exponential.

The relationship between variables was named as Karva expression by Candida Ferreira (Ferreira, 2001b, 2001a) who developed the GEP algorithm. For predicting at different ages of $f_c$, values of SCC produced with FA, the developed ETs, the GEP-I model with 4-Sub-ETs (4-genes or 4-Sub-ETs) and the GEP-II model with 5-Sub-ETs (5-genes or 5-Sub-ETs) were given in Figures 2 and 3, respectively. The purpose of using two different models is to find the model that gives the best results with the effect of the Sub-ETs (genes number). The large number of input variables in both models led to the use of too many ETs and too long chromosome structures. The Karva expressions, which compose of the ETs of the models developed from the GEP-I and the GEP-II, were given in Equations 1 and 2. Moreover, according to ETs, the formula attained from the GEP-I model was presented in Equations 3 and 4, while that of the GEP-II model was presented in Equations 5 and 6. The symbols seen in ETs: $d_0 = C$, $d_1 = W$, $d_2 = FA$, $d_3 = C_{agg}$, $d_4 = F_{agg}$, $d_5 = SP$ and $d_6 = AS$ are denote the input variables. The constants indicated by $c_i$ ($i = 1, 2, ..., 9$) in the Sub-ETs in the GEP models were given in Table 3. If the necessary constants and input variables are substituted in Equations 3 and 5, the simplified formulas obtained from the GEP-I and the GEP-II models are as presented in Equations 4 and 6. After obtaining these formulas, the validations of them were made with 148 independent data obtained from the literature, which were not employed in the training and testing sets of the models.

### Equations

\[
\begin{align*}
&+.d0.c9.Ln.X2.X2./.d6.c9.c2 \\
&*Inv.Add3.+.c5.d1.Tan.Exp.+d5.+d0.d1.c3 \\
\end{align*}
\]

(1)

\[
\begin{align*}
f_{c-pred.1} &= (((d1/c7)+(d0+d2+d0)+d1)+((d6*c9)+(d4/c0))+((d5*d5)*(Csc(c1)))) \\
&*((d0-[Csc((d5+c8)*(c6-d3)*Tan(d4))]*(c8*c7)))) \\
&*((Ln(d6)^2)*((c9/c2)^2)*d0+c9) \\
&*(1/((d3-((c4+d0)*d1+d6+c8)*d1)*Tan(Sin(c4)))) \\
\end{align*}
\]

(3)

\[
\begin{align*}
f_{c-pred.2} &= (2CA+0.44W+4.933AS+0.25F_{agg}-18.438SP^2) \\
&*(C-Csc((SP-5.135)*(6.829-C_{agg})*(Tan(F_{agg})*(37.532)))) \\
&*((Ln(AS)^2)*103.276)*(C-84.44) \\
&*(1/((C_{agg}*((24.575+C)*(W+AS+5.304)*W)*0.007))) \\
\end{align*}
\]

(4)

350
Figure 2. Expression tree for the empirical model obtained from the GEP-I. Source: Self-elaboration.

\[ f_{c-pred-II} = ((\text{Sqrt}(d2 \cdot d3 \cdot d0)) - (d4 \cdot d1 \cdot d5) \cdot (d2 \cdot d5 \cdot c8)) - ((d0 + c4 + d0) \cdot (d3 - c4)) \]
\[ \cdot (1/(((c6 - 1/(((d3 - c1) - d6)))) \cdot (c6^2) \cdot c4)) \]
\[ \cdot (d5 + 27.585) - ((2C - 124.752) \cdot (C_{agg} + 124.752)) \]
\[ \cdot (1/(6.280 - 1/(((C_{agg} \cdot 0.839) - FA - AS)))) \cdot (393.280)) \]
\[ \cdot (W - 1.208) + \text{Exp}(W) - 39.00 + W) \]
\[ \cdot (-5.48 + \text{Cos}((C + 4.99) \cdot (C_{agg} - 17.362)) \cdot (1/(C - 2F_{agg}) \cdot C_{agg}) \]
\[ \cdot (\text{Ln}(AS + Tan(C_{agg} + 8.681 \cdot AS))) \]
Table 3. Fixed numbers employed in the GEP. Source: Self-elaboration.

<table>
<thead>
<tr>
<th>Sub-ETs</th>
<th>Constants</th>
<th>GEP-I</th>
<th>GEP-II</th>
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Figure 3. Expression tree for the empirical model obtained from the GEP-II. Source: Self-elaboration.
Performances of GEP models

In this modelling study, some statistical parameters were employed in the evaluation of performance of the formulas derived from the models in the GEP for estimating the $f_c$ of SCC produced with FA. These statistical parameters were the mean absolute percentage error (MAPE), root mean square error (RMSE) and R-square ($R^2$). They were presented in Equations 7, 8 and 9, respectively. These equations were used to compare and evaluate the $f_{c\text{-exp.}}$ results of experimental works and the $f_{c\text{-pred.}}$ results of formulas attained from the models evolved in the GEP.

$$MAPE = \frac{1}{n} \left[ \frac{1}{n} \sum_{i=1}^{n} \left| \frac{f_{c\text{-exp.},i} - f_{c\text{-pred.},i}}{f_{c\text{-exp.},i}} \right| \times 100 \right]$$ \quad \text{(7)}$$

$$RMSE = \sqrt{\frac{1}{n} \sum_{i=1}^{n} \left( f_{c\text{-exp.},i} - f_{c\text{-pred.},i} \right)^2}$$ \quad \text{(8)}$$

$$R^2 = \frac{\left( n \times \sum_{i=1}^{n} f_{c\text{-exp.},i} \times f_{c\text{-pred.},i} \right)^2 - \left( \sum_{i=1}^{n} f_{c\text{-exp.},i} \times \sum_{i=1}^{n} f_{c\text{-pred.},i} \right)^2}{\left( n \times \sum_{i=1}^{n} f_{c\text{-exp.},i} \right)^2 - \left( \sum_{i=1}^{n} f_{c\text{-exp.},i} \right)^2 \times \left( n \times \sum_{i=1}^{n} f_{c\text{-pred.},i} \right)^2}$$ \quad \text{(9)}$$

Where, $f_{c\text{-exp.}}$ is the target value attained from the experimental studies, $f_{c\text{-pred.}}$ is the output value obtained from the formulas and $n$ is the number of experimental data.

Results and comparisons of GEP models

The $f_{c\text{-pred.}}$ values attained from training and testing sets of both GEP models and the ANN (Golafshani & Pazouki, 2018) models, and obtained from versus the $f_{c\text{-exp.}}$ values achieved from the experimental works of the SCC with FA are given in Figures 4 and 5. In addition, the error values between the estimated results for both GEP models and the experimental work results are shown in Figures 6 and 7. The $f_{c\text{-pred.}}$ values handled from the training and testing sets in both GEP models are very close to the experimental work results as seen in Figures 4 and 5. This closeness can be clearly seen by the $R^2$ values as given in Figures 4 and 5. Moreover, as seen in Figures 6 and 7, the error values between the estimated results for both GEP models and the experimental study results are very low. This situation shows the availability of formulas developed. Herein, when both GEP models are compared in terms of closeness to experimental results, the GEP-II model results are closer than that of GEP-I model ones. The number of genes (sub-ETs) used in the GEP-II model appears to be effective in this closeness. However, increasing the number of genes in the model causes the proposed formula more complex and diminish its usability. When the GEP models and the proposed ANN model are compared, it can be seen that the results of the ANN model are more appropriate to the experimental work results than that of the GEP models. On the other hand, in the proposed ANN model, there is no general formula that can be used by everyone like GEP models. Unused data in the training and testing sets of these models were used to measure the generalization capacity of the formulas obtained from the GEP models. This used data is also expressed as a validation set. The comparison of the results obtained from the validation set of the formulas obtained from both GEP models with the experimental study results is shown in Figure 8. Furthermore, the error values between the results obtained from the validation set of the formulas attained from the GEP models and the experimental results are given in Figure 9. The
validity and generalization capacity of the formulas given in Equations 4 and 6 attained from the GEP-I and the GEP-II models were verified by the validation set. This validation set underlines the main difference between GEP models and ANN ones.

**Figure 4.** Comparison of experimental and predicted results for training set. Source: Self-elaboration.

**Figure 5.** Comparison of the experimental and predicted results for testing set. Source: Self-elaboration.

**Figure 6.** Error values between the experimental and predicted results for training set. Source: Self-elaboration.
In this modelling study, the performances of both GEP models and the proposed ANN model (Golafshani & Pazouki, 2018) were also evaluated by MAPE, RMSE and $R^2$ statistical parameter values. While the results of these statistical parameters for training, testing and validation sets used in both GEP models are given in Table 4, they could not be given for ANN model owing to have no validation set. According to the results of these statistical parameters, the developed GEP models can be employed to estimate the $f_c$ values of SCC produced with FA at various ages.

When the GEP models were compared according to MAPE values, the highest MAPE value is 24.531 for the validation set of the model attained from the GEP-II, and the lowest MAPE value is 18.658 for the training set of the model attained from the GEP-II. Similarly, the highest RMSE value is 9.109 for the validation set of the model attained from the GEP-II, and the lowest RMSE value is 6.304 for the training set of the model attained from the GEP-II. $R^2$ of both GEP models for the sets are larger than 0.777, as given in Table 4. When the models attained from the GEP were compared in reference to $R^2$ values, the best $R^2$ value is 0.892 for the training set of the model attained from the GEP-II as the lowest $R^2$ value of is 0.777 for the validation set of the model attained from the GEP-II. The statistical parameter values show that $f_c$ values of SCC produced...
with FA can be estimated by these formulas and these formulas can be used by everyone. The $R^2$ values of the ANN model developed by Golafshani and Pazouki (Golafshani & Pazouki, 2018) are larger than that of the GEP models. However, in the previously proposed ANN model according to the formulas obtained from GEP models, there is no suggested an equation that everyone can use. In this respect, it is thought that GEP models may have more widespread effects than the previously proposed ANN model. The results of validation set show that the formulas obtained by using GEP models are able to be generalized among the output and inputs. Moreover, the $f_i$ values of the SCC with FA can be closely predicted to the experimental results in a short time by using the formulas obtained from these models.

| Table 4. Results of parameters used to evaluate of models. Source: Self-elaboration. |
|---------------------------------------------------------------|-----------------|----------------|---------------|
| **MAPE** | **RMSE** | **$R^2$** |
| **Training** | **Testing** | **Validation** | **Training** | **Testing** | **Validation** | **Training** | **Testing** | **Validation** |
| GEP-I | 19.826 | 20.157 | 21.792 | 7.211 | 7.983 | 8.760 | 0.859 | 0.840 | 0.785 |
| GEP-II | 18.658 | 22.561 | 24.531 | 6.304 | 7.411 | 9.109 | 0.892 | 0.860 | 0.777 |
| ANN | 10.592 | 17.834 | - | 3.405 | 5.849 | - | 0.968 | 0.924 | - |

Conclusions

In this modelling study, the formulas attained from the GEP-I and GEP-II models developed by utilizing GEP technique were employed to estimate $f_i$ values of SCC produced with FA at various ages. The input and output variables attained from experimental studies were employed in the training and testing sets of the models developed in GEP technique. Then, the formulas obtained from these models validated by using the input variables obtained from experimental studies, which are not used in the training and testing sets of the models. The results of sets of the models showed that the $f_{i_{exp}}$ results of the SCC produced with FA at different ages could be closely predicted with proposed formulas. The values of $f_{i_{exp}}$ from the experimental studies and $f_{i_{pred}}$ which are attained from the sets of the GEP model are close to each other. This closeness can be explained in terms of MAPE, RMSE and $R^2$ statistical parameter values for two novel mathematical formulas based on the models attained from the GEP-I and GEP-II. Thus, the $f_i$ values of SCC produced with FA at different ages can be estimated in a short period with very small error rates by utilizing the equations obtained from GEP models.

References


